

Name: _____ Matric #: _____

You do not need to simplify nor numerically evaluate the expressions for your answers:

1. Two Frames A & B are initially coincident. Frame A is fixed, while Frame B moves according to the following sequence:
 - i) Rotation about X_A of 30 degrees
 - ii) Rotation about Y_B of 60 degrees
 - iii) Rotation about Z_A of 90 degrees, and
 - iv) Translation of (1,2,3) along Frame B.

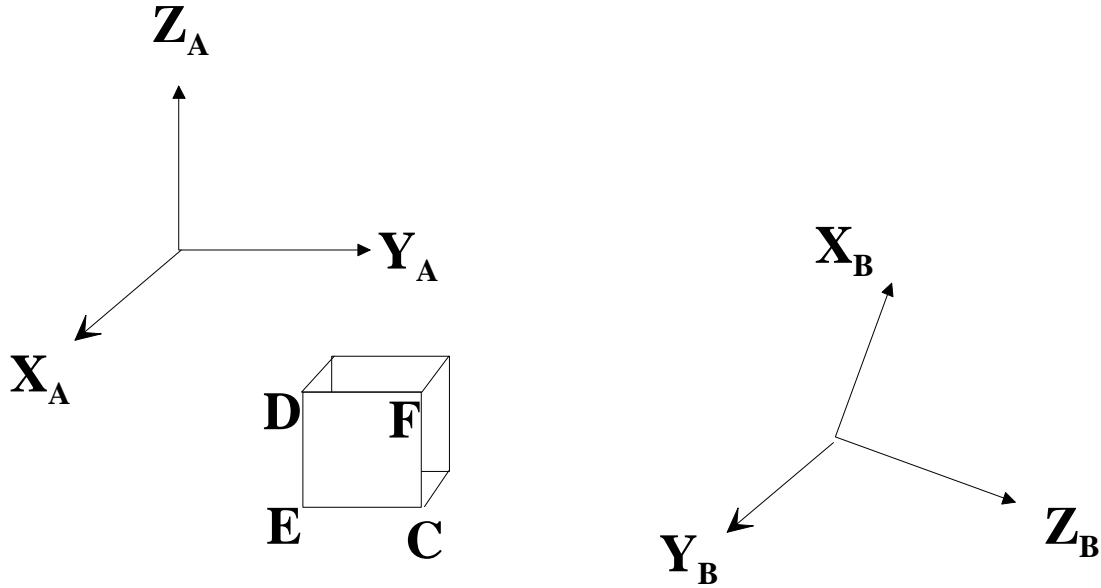
Find the new position and orientation of Frame B in Frame A. (Express this as a homogeneous transformation matrix.

Ans:

$$T = \text{Rot}(z, 90^\circ) \text{Rot}(x, 30^\circ) \text{Rot}(y, 60^\circ) \text{Trans}(1,2,3)$$

(please turn over)

2. In the figure below, the origin of frame B is at (5,10,-3) with respect to Frame A, and the corner C of the cube is at (6, 7,1) with respect to Frame A. The cube has a side of dimension 1 unit. The DECF face the cube, yz plane of Frame A and xz plane of Frame B are all parallel. The cube is rotated by 30 degrees about Y_B . Find the new coordinates of E in Frame A after this rotation.



Ans:

$${}^A P_E = (6 \ 6 \ 1 \ 1)^T$$

$${}^A P_E = {}^A T_B \text{Rot}(y, 30^\circ) {}^B T_A {}^A P_E$$